

# IGP

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1. Consider rectangle  $ABCD$  with  $AB = 6, BC = 8$ . Let  $M$  be the midpoint of  $AD$  and let  $N$  be the midpoint of  $CD$ . Let  $BM, BN$  intersect  $AC$  at  $X, Y$ . Find  $XY$ . (W1)
2. Prove  $[ABC] = rs$ . (1.5)
3. Consider  $\triangle ABC$  with  $AB = 5, BC = 12, AC = 13$ . Angle bisector  $AD$  and median  $AE$  is drawn such that  $B, C, D, E$  are collinear. Find  $[ADE]$ . (2.2)
4. Simplify  $(1+x)(1+x^2)(1+x^4)(1+x^8)(1+x^{16})$ . (3.3)
5. If  $f(x) = \frac{x^2}{x^2-1}$ , find  $\prod_{n=3}^{50} f(n)$ . (3.6)
6. Find the number of subsets of  $\{1, 2, 3, 4, 5, 6, 7, 8\}$  that are subsets of neither  $\{1, 2, 3, 4, 5\}$  nor  $\{4, 5, 6, 7, 8\}$ . (4.4)